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SIDDHARTH INSTITUTE OF ENGINEERING & TECHNOLOGY:: PUTTUR
(AUTONOMOUS)

B.Tech I Year I Semester Supplementary Examinations November 2020

Engineering Mathematics-I

(Common to all)

Time: 3 hours

Max. Marks: 60

(Answer all Five Units 5 x 12 = 60 Marks)

UNIT-I

- 1 a Solve $x \frac{dy}{dx} + y = \log x$ 6M
- b Solve $\frac{dy}{dx} + y \tan x = y^2 \sec x$ 6M

OR

- 2 Solve $(D^3 + 2D^2 + D)y = e^{2x} + x + \sin 2x$ 12M

UNIT-II

- 3 a If $u = \frac{yz}{x}; v = \frac{zx}{y}; w = \frac{xy}{z}$, show that $\frac{\partial(u, v, w)}{\partial(x, y, z)} = 4$ 6M
- b Expand $\log(1+ex)$ in ascending powers of x 6M

OR

- 4 a Find the radius of curvature at the origin for the curve $y^4 + x^3 + a(x^2 + y^2) - a^2y = 0$ 6M
- b Find the minimum value of $x^2 + y^2 + z^2$ given $x + y + z = 3a$ 6M

UNIT-III

- 5 a Find $\iint (x^2 + y^2) dx dy$ over the area bounded by the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ 6M
- b Evaluate the following integral by transforming into polar coordinates 6M
- $$\int_0^\infty \int_0^\infty e^{-(x^2+y^2)} dx dy$$

OR

- 6 a Evaluate $\int_1^e \int_1^{\log y} \int_1^{e^x} \log z dz dx dy$ 6M
- b Show that by the double integration, the area between the parabolas $y^2 = 4ax$ and $x^2 = 4ay$ is $16a^2/3$ 6M

UNIT-IV

- 7 a Find the Laplace transform of $3\cos 3t \cos 4t$ 6M
- b Find the Laplace transform of $e^{-3t} (2 \cos 5t - 3 \sin 5t)$ 6M
- OR**
- 8 a Find the Laplace transform of $f(t) = t \sin 3t \cdot \cos 2t$ 6M

- b Find $L\{F(t)\}$, where $F(t)$ is a periodic function of period $2a$ and it is given by $F(t) = \begin{cases} k & 0 < t < a \\ -k & a < t < 2a \end{cases}$ 6M

UNIT-V

9 a Find the Inverse Laplace Transform of $\frac{5s-2}{s^2(s+2)(s-1)}$ **6M**

b Find $L^{-1}\left\{\frac{1}{2}\log\left(\frac{s^2+b^2}{s^2+a^2}\right)\right\}$ **6M**

OR

10 Using Laplace Transform method,
solve $(D^2 + n^2)x = a \sin(nt + \alpha)$, $x = Dx = 0$ at $t = 0$ **12M**

*** END ***